

Augmenting Global Real-Time PPP Service With Regional Network For Instantaneous cm-Level Positioning

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Network Real-Time Kinematic (NRTK)

- Using a local/regional reference network
- OBS. DOMAIN Representation

NRTK Service Covers The Whole European/Chinese Territory?

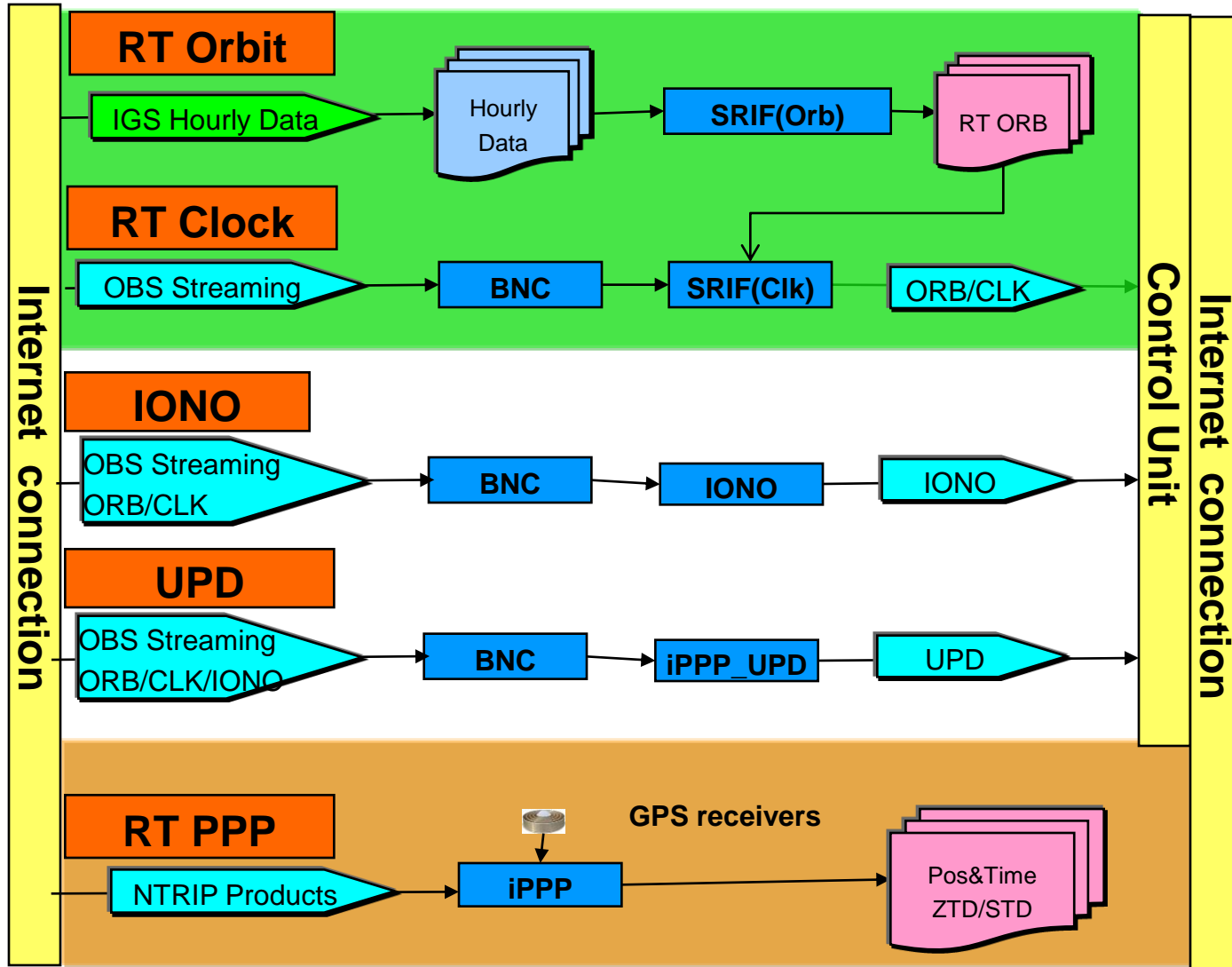
Global Precise Point Positioning Service

- Using a global reference network
- STATE DOMAIN Representation

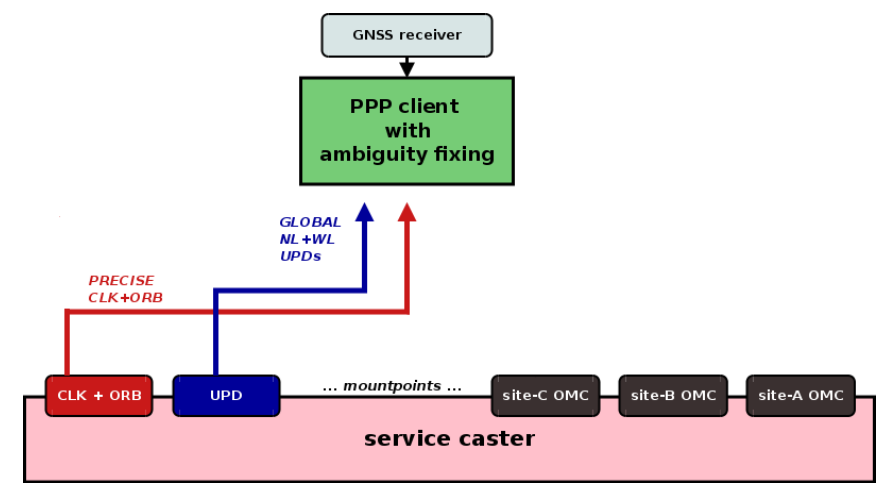
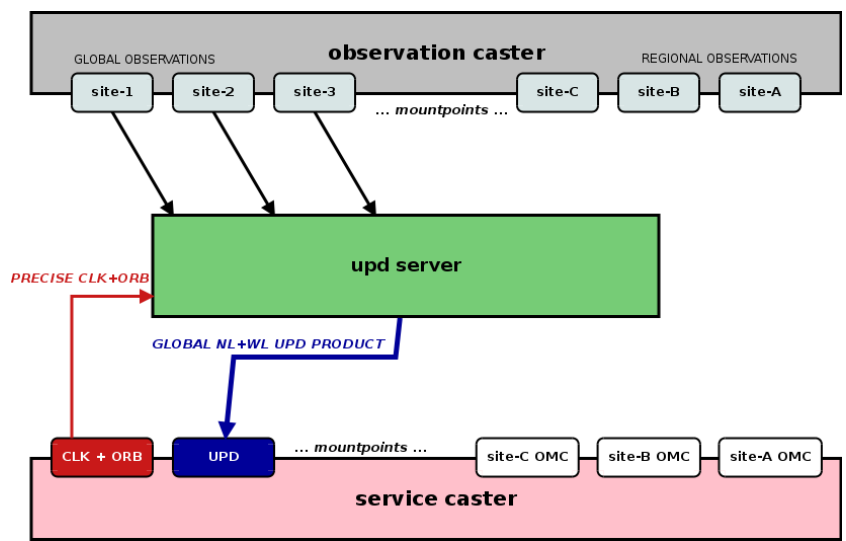
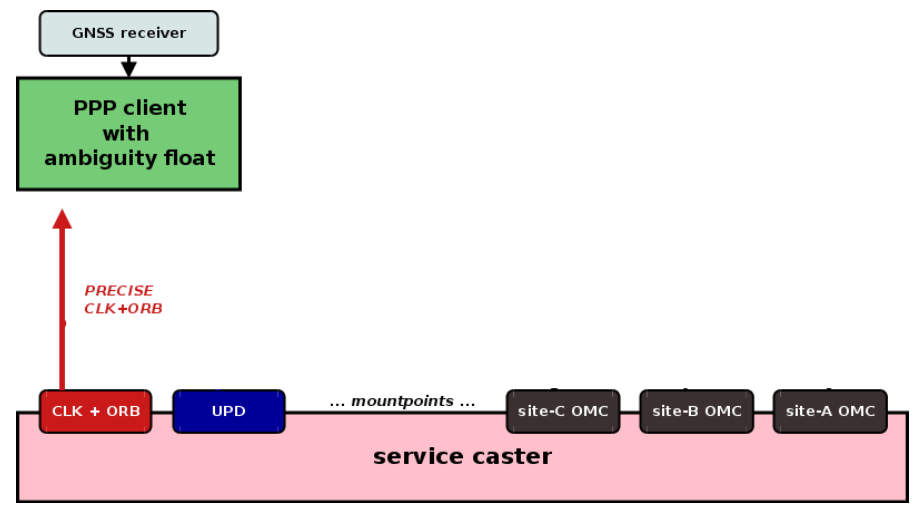
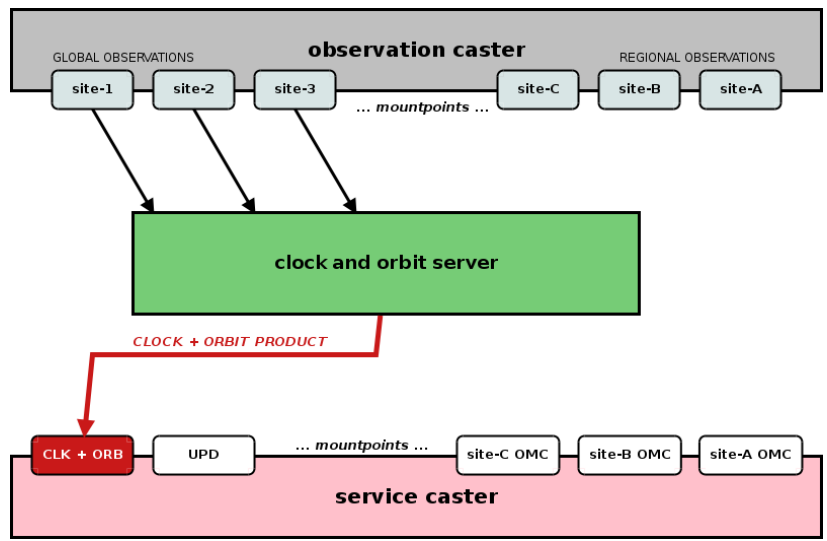
Initialization/Re-initialization takes 10-30 Min..

**Global PPP + Regional Augmentation For All
Real-Time Applications**

IGS Real-Time Analysis Center at GFZ



Standard PPP & PPP + AmbFixing



PPP Ambiguity Resolution

➤ Estimation of UPDs

$$b_{mk}^i = n_{mk}^i + \Delta\phi_m^i - \Delta\phi_{mk} \quad \text{➤ With Integer } N_i$$

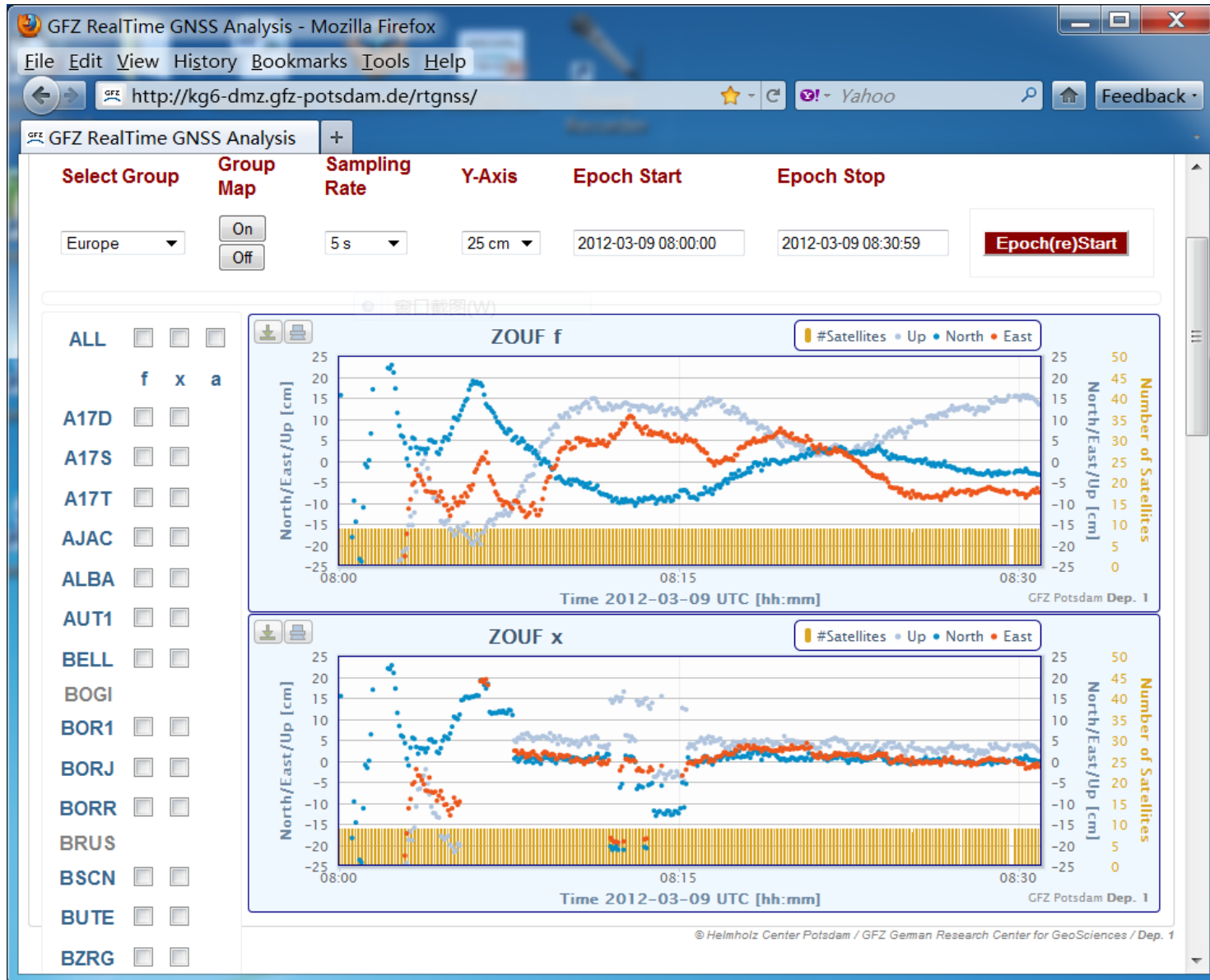
$$\begin{bmatrix} \mathbf{b}_1 \\ \mathbf{b}_2 \\ \vdots \\ \mathbf{b}_n \end{bmatrix} = \begin{bmatrix} \mathbf{I} & & & \mathbf{R}_1 & \mathbf{S}_1 \\ & \mathbf{I} & \mathbf{0} & \mathbf{R}_2 & \mathbf{S}_2 \\ & & \mathbf{I} & \vdots & \vdots \\ \mathbf{0} & & & \mathbf{I} & \mathbf{R}_n \\ & & & & \mathbf{S}_n \end{bmatrix} \begin{bmatrix} \mathbf{n}_1 \\ \mathbf{n}_2 \\ \vdots \\ \mathbf{n}_n \\ \Delta\phi_{\mathbf{R}} \\ \Delta\phi_{\mathbf{S}} \end{bmatrix}, \quad \mathbf{Q}_{\text{bb}}$$

$$\begin{bmatrix} \mathbf{b}_1 - \mathbf{n}_1 \\ \mathbf{b}_2 - \mathbf{n}_2 \\ \vdots \\ \mathbf{b}_n - \mathbf{n}_n \end{bmatrix} = \begin{bmatrix} \mathbf{R}_1 & \mathbf{S}_1 \\ \mathbf{R}_2 & \mathbf{S}_2 \\ \vdots & \vdots \\ \mathbf{R}_n & \mathbf{S}_n \end{bmatrix} \begin{bmatrix} \Delta\phi_{\mathbf{R}} \\ \Delta\phi_{\mathbf{S}} \end{bmatrix}$$

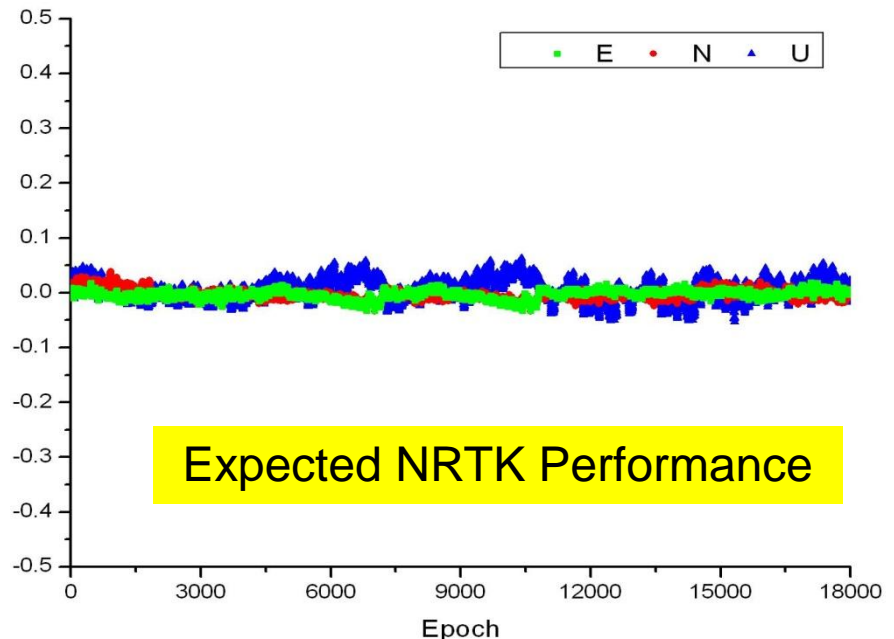
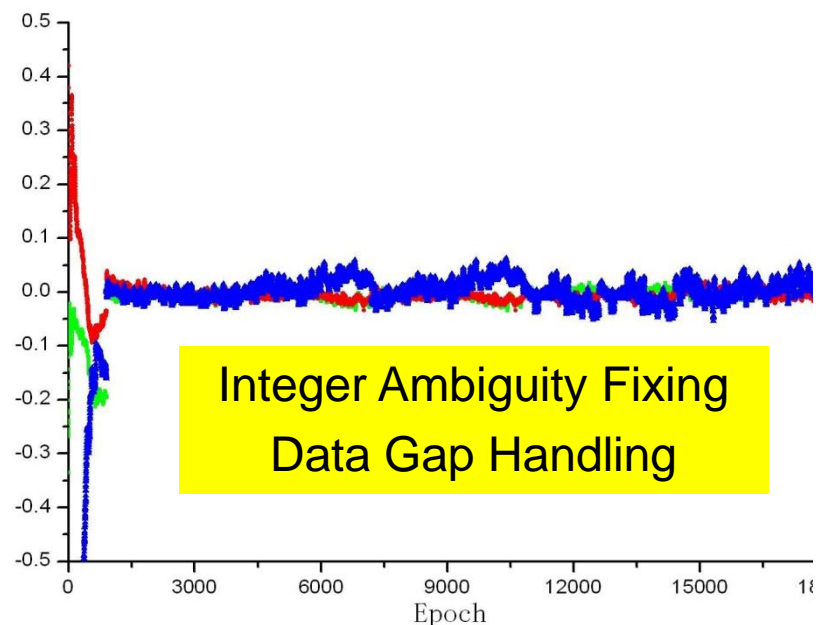
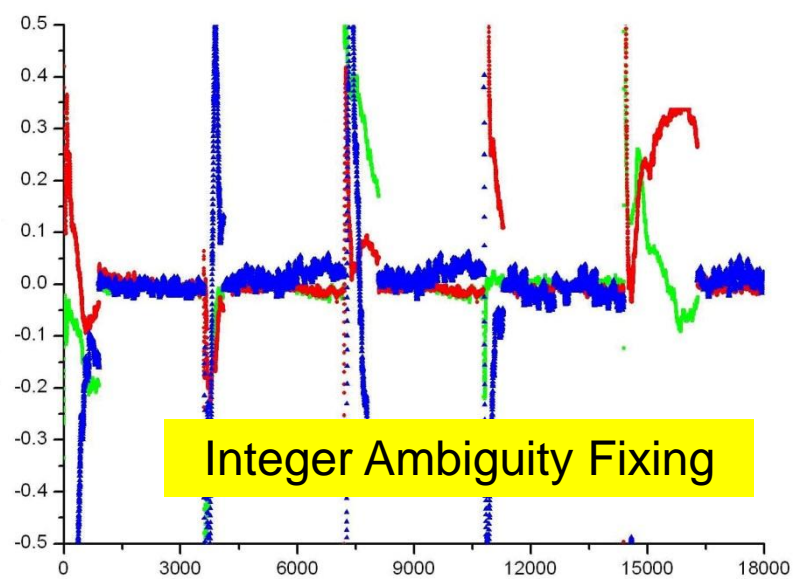
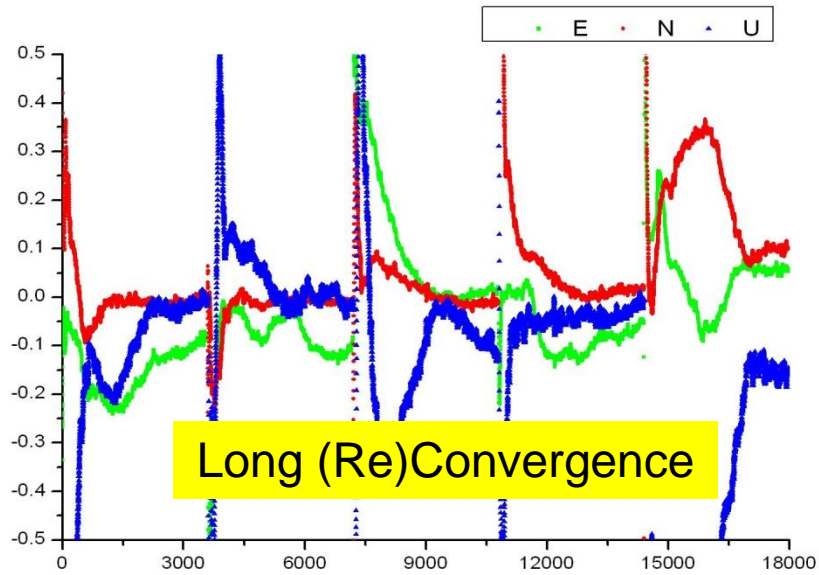
➤ Algorithm

1. Get Initial $\Delta\phi_{mk}$ $\Delta\phi_m^i$
2. Fix Integer Ambiguities n_{mk}^i
3. Remove IA, Solve For $\Delta\phi_{mk}$ $\Delta\phi_m^i$
4. Repeat Above Procedure

Typical Performances



Typical Performances



Regional Augmentation vs Network RTK

- Global PPP Service Is Needed
- Using Undifferenced Obs. Corrections – Break Down Rec.&Sat. Connections
- Casted Station-By-Station – No Communication Bottleneck
- Network Solution Not A Must – Unlimited Number Of Reference Stations

Principal: Unambiguous OMC

➤ OMC of Station k to Satellite i

$$\begin{aligned}
 omc_k^i &= L_k^i - \tilde{\rho}_k^i && \delta S_k^i \text{ Orbit Bias} \\
 &= \delta S_k^i - \delta t^i + \delta t_k + \delta I_k^i && f_k \text{ UPD Receiver} \\
 &\quad + \delta T_k^i + n_k^i + f_k - f^i && f^i \text{ UPD Satellite}
 \end{aligned}$$

➤ Unambiguous OMC (Ambiguity Known)

$$\begin{aligned}
 l_k^i &= omc_k^i - n_k^i \\
 &= \delta S_k^i - \delta t^i + \delta t_k + \delta I_k^i + \delta T_k^i + f_k - f^i
 \end{aligned}$$

➤ Interpolated User Correction

Interpolated Correction	User Obs. Equ.	Cor. Obs. Equ.
$\bar{l}_u^i = \sum_{k=1}^3 \alpha_k (\delta S_k^i + \delta I_k^i + \delta T_k^i)$ $+ \sum_{k=1}^3 \alpha_k (\delta t_k + \delta f_k)$ $- \delta t^i - \delta f^i$ <p>With $\alpha_1 + \alpha_2 + \alpha_3 = 1$</p>	$l_u^i = \delta S_u^i + \delta I_u^i + \delta T_u^i$ $+ \delta t_u + \delta f_u$ $- \delta t^i - \delta f^i + n_u^i$ $+ u_u^i \delta x_u$	≈ 0 $= \text{Contant}$ $= n_u^i$ $= u_u^i \delta x_u$

➤ **Corrected Obs. Equ == PPP With Integer SD-Ambiguities**

➤ **How To Get The Integer UD-Ambiguities For L1&L2 ?**

- **NRTK With UD-Corrections**
Based On Fixed DD-Ambiguities
- **PPP Augmentation,**
Based On Fixed UD-Ambiguities

Unambiguous UDOMC From PPP

- After PPP For All Stations, We Have

$$b_k^i = n_k^i + f_k - f^i$$
- Solve for f_k , f^i , then n_k^i as explained
- With n_k^i , UD OMCs are derived.
- n_k^i Can Be Biased Because f_k , f^i Are Usually Biased By Integers

Unambiguous UDOMC From PPP

- Assume that f_i, f^k Are Biased By Integers

$$\begin{bmatrix} \bar{l}_u^1 \\ \bar{l}_u^2 \\ \bar{l}_u^3 \end{bmatrix} = \left(\begin{bmatrix} l_1^1 & l_2^1 & l_3^1 \\ l_1^2 & l_2^2 & l_3^2 \\ l_1^3 & l_2^3 & l_3^3 \end{bmatrix} - \begin{bmatrix} \delta f_1 - \delta f^1 & \delta f_2 - \delta f^1 & \delta f_3 - \delta f^1 \\ \delta f_1 - \delta f^2 & \delta f_2 - \delta f^2 & \delta f_3 - \delta f^2 \\ \delta f_1 - \delta f^3 & \delta f_2 - \delta f^3 & \delta f_3 - \delta f^3 \end{bmatrix} \right) \begin{bmatrix} \alpha_1 \\ \alpha_2 \\ \alpha_3 \end{bmatrix}$$

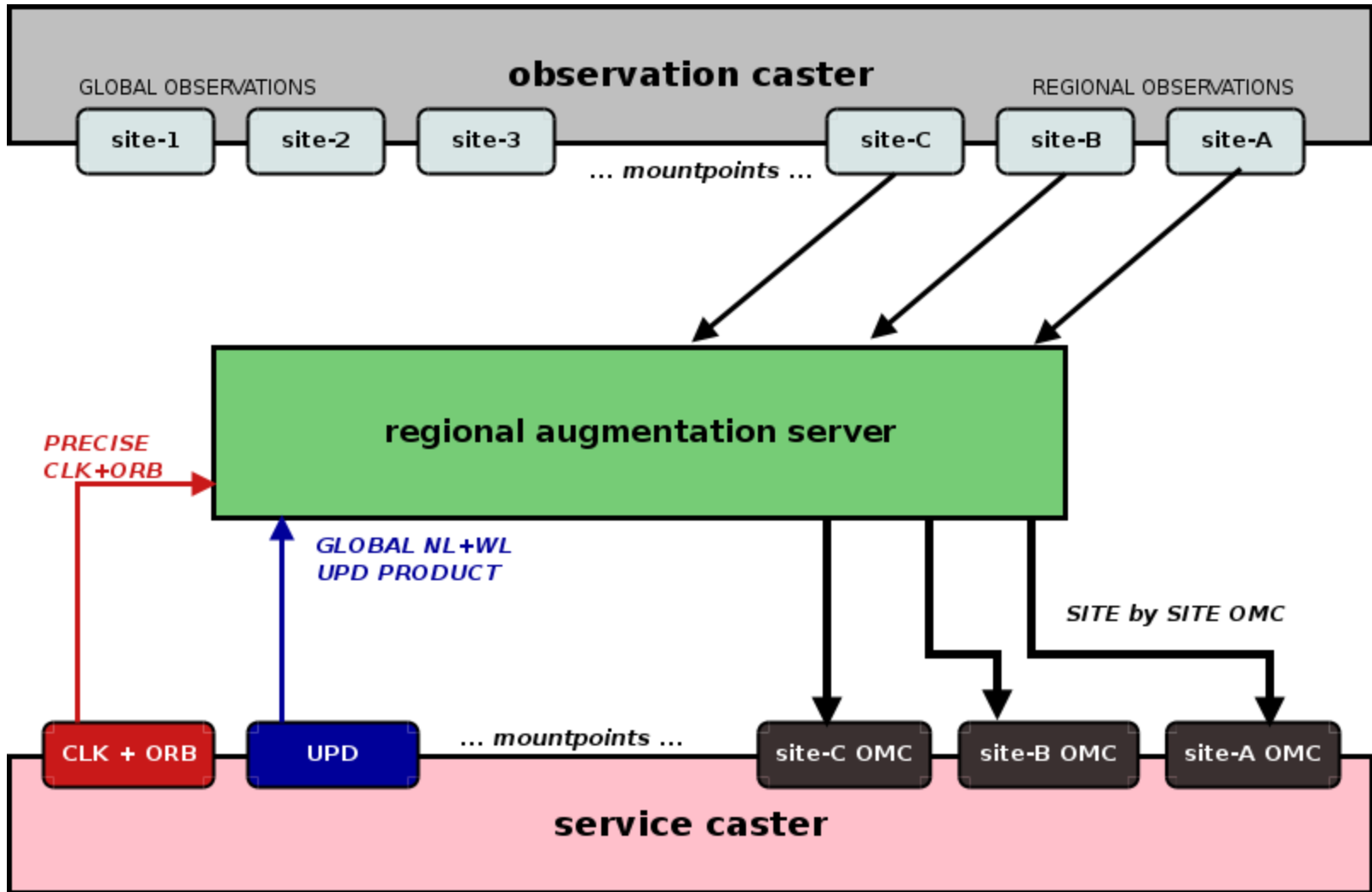
- Biases in the Interpolated Corrections

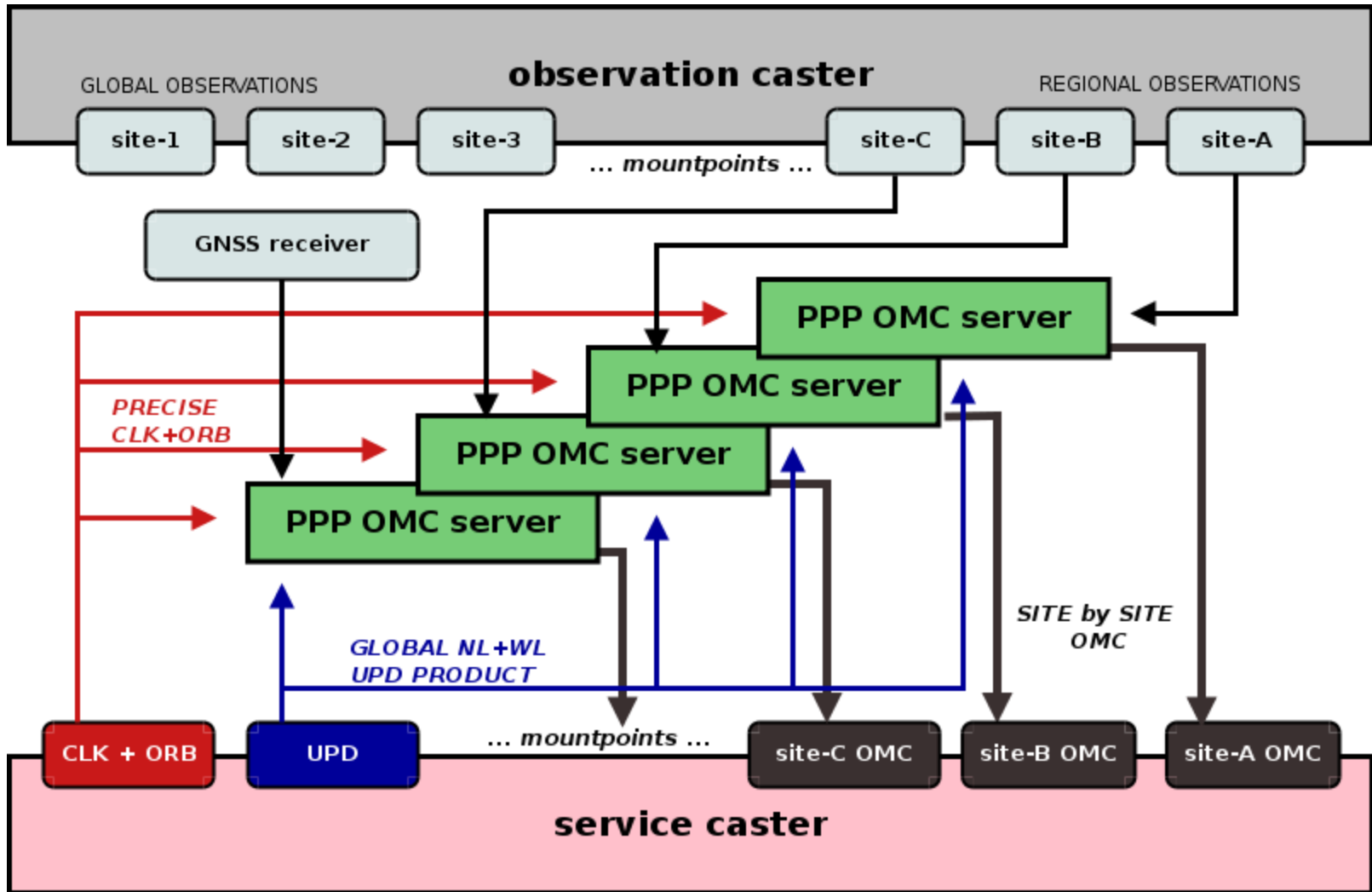
$$\begin{bmatrix} \delta \bar{l}_u^1 \\ \delta \bar{l}_u^2 \\ \delta \bar{l}_u^3 \end{bmatrix} = \sum_{i=1}^3 \alpha_i \delta f_i \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix} - \begin{bmatrix} \delta f^1 \\ \delta f^2 \\ \delta f^3 \end{bmatrix}$$

Satellite-specific, constant
for all related epochs

A constant for all satellites

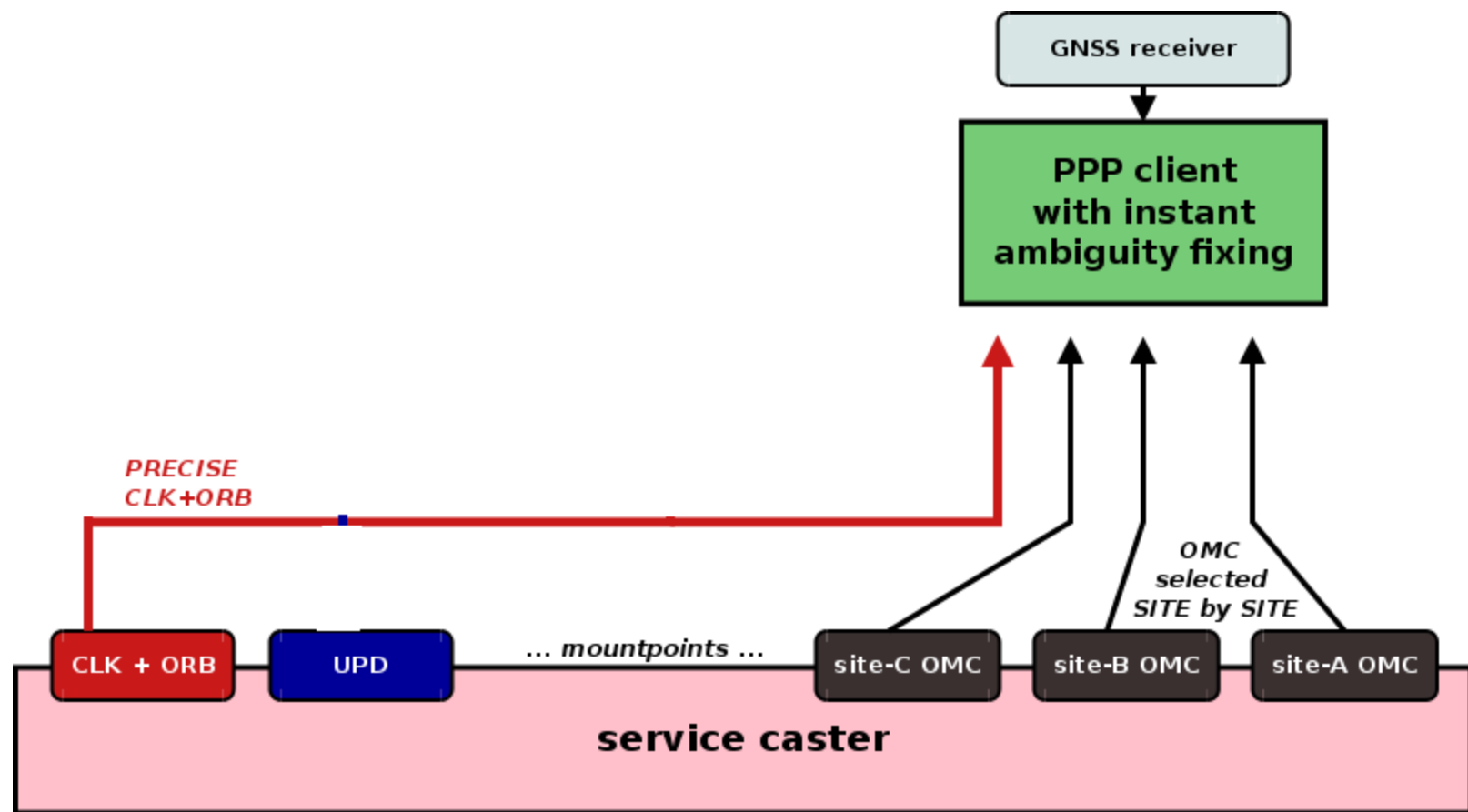
- The 1st. a constant for all sats, and the 2nd, a integer constant for each sat, both will be absorbed by ambiguities
- SD ambiguities are natural integer.





➤ Network Solution Not A Must

PPP+Regional Augmentation Client



➤ **PPP with Raw Observations**

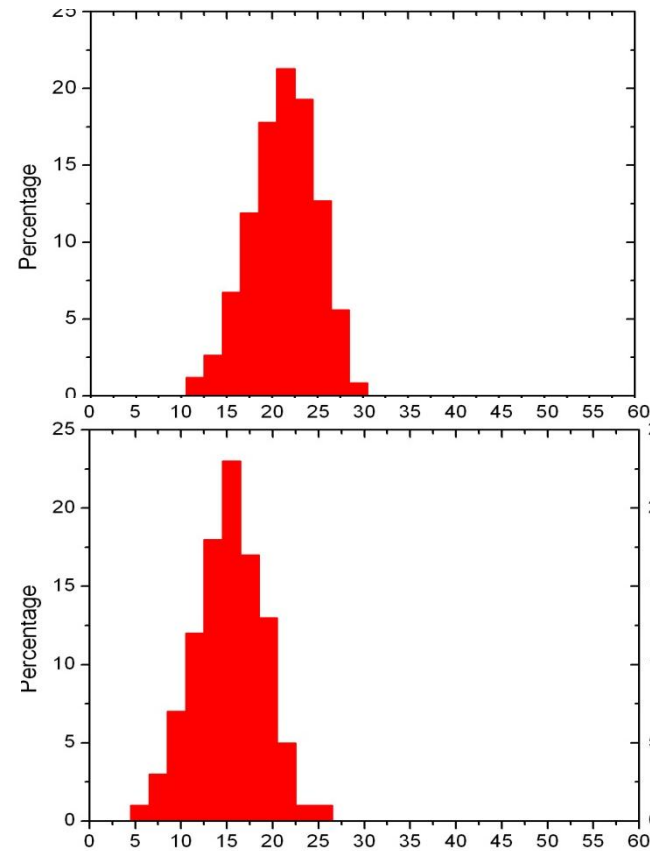
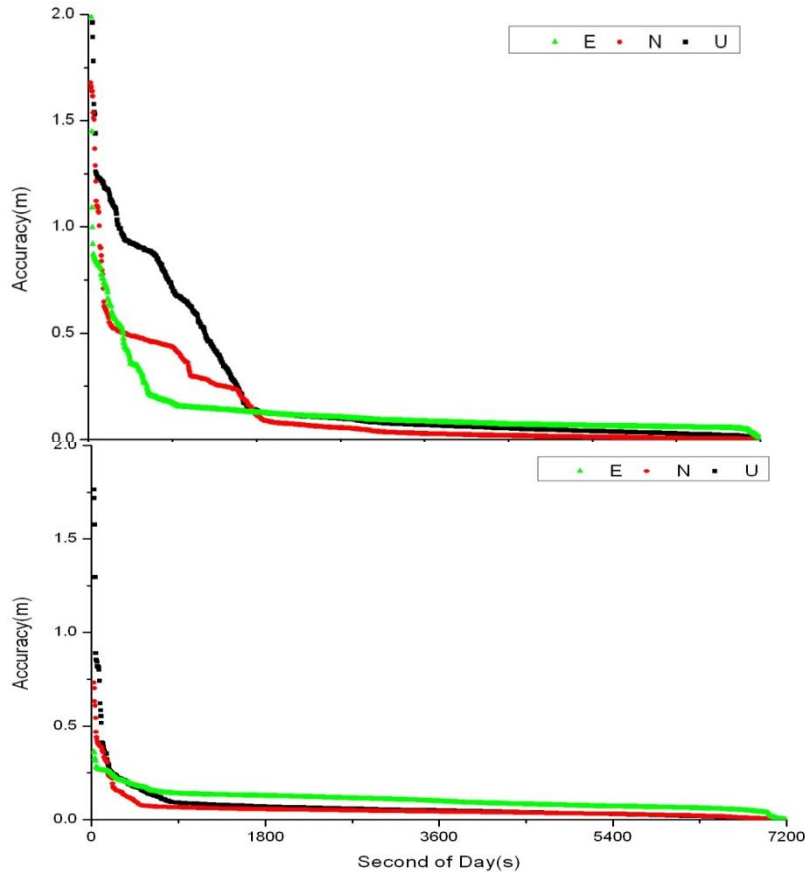
- Ionospheric Trace Delays Are Estimated

➤ **Ionospheric Constraints**

- Spatial Constraint (Gradients)
- Temporal Constraint (Random-Walk Process)
- Ionospheric Correction Constraint (Pseudo-obs.)

ION 2012 Student Award Winner, Mr. Xingxing LI
IONO. Model, Presented By Dr Hongping Zhang

PPP With Iono. Constraints (Ref)



➤ Improvements

- Faster Convergence, 30 to 20 min < 10 cm
- Faster Ambiguity-Fixing, 20 to 15 min
- Static Station, 10 min, **With Known Position, 5 min**

➤ **PPP with Raw Observations**

- Corrections From Ref. Stations Applied
- Remaining Ionospheric Trace Delays Estimated

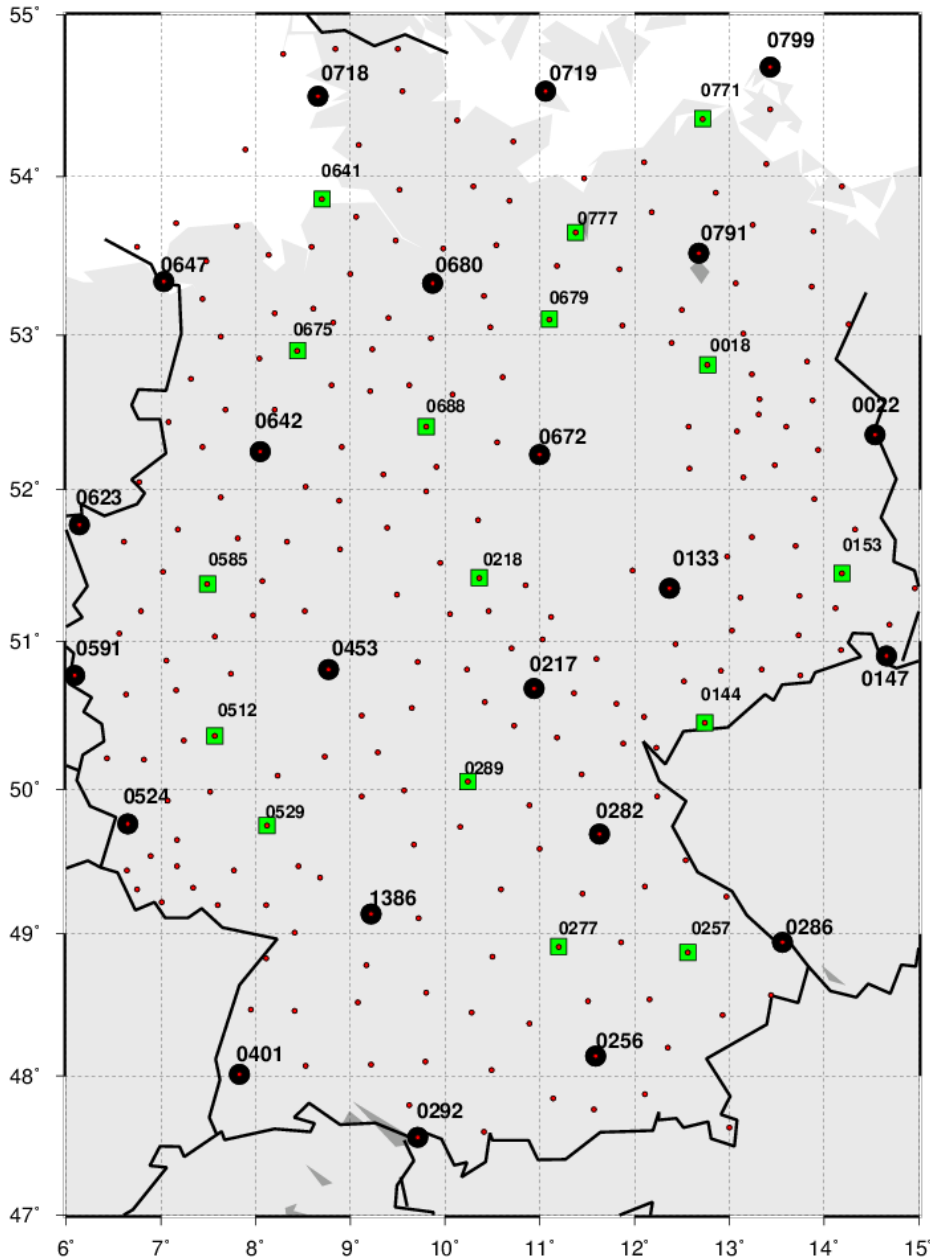
➤ **Ionospheric Constraints**

- Spatial Constraint (Gradients)
- Temporal Constraint (Random-Walk Process)

➤ **Improvements**

- Ambiguity-Fixing At User-End
- Larger Inter-Station Distance

Real-Time Validation (SAPOS)



➤ DATA

- SAPOS Real-Time Data of about 200 stations (2012) among them about 20 GREF stations
- Various receiver types
- 1 seconds sampling rate

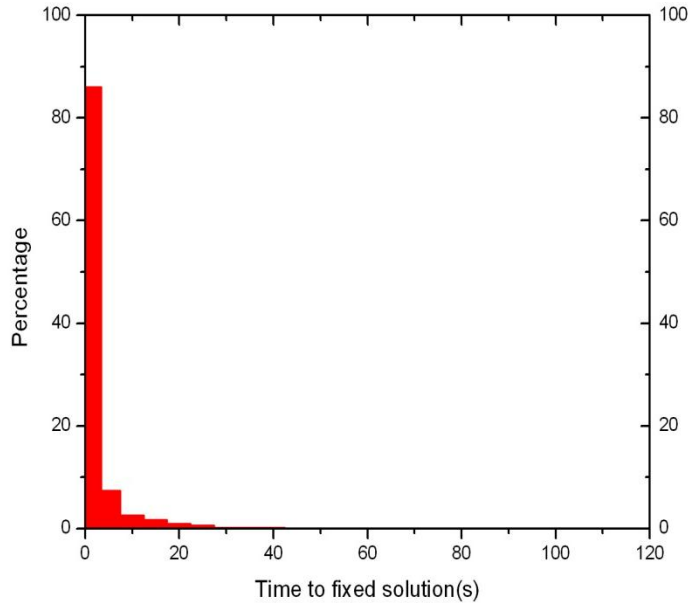
➤ Reference Network

- Selected 22 reference stations
- Inter-station distance 180 km
- 17 user stations (green squares)

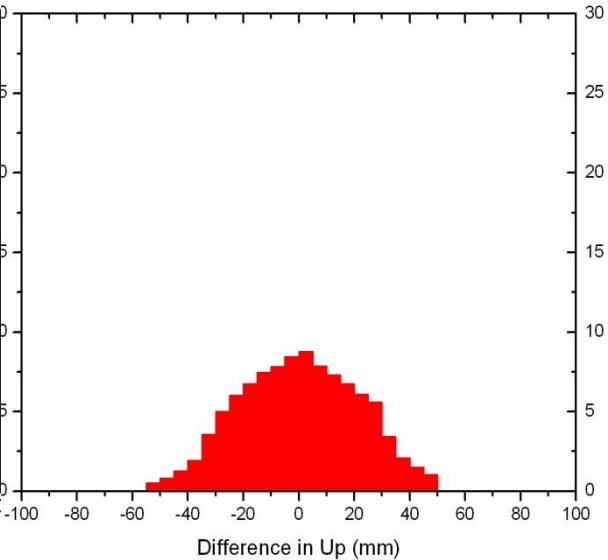
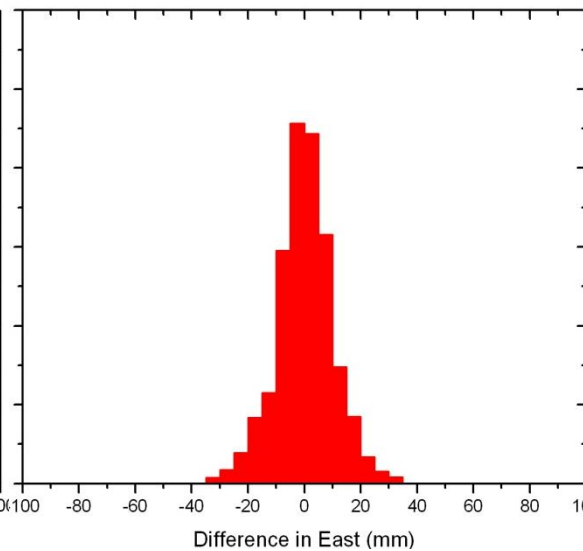
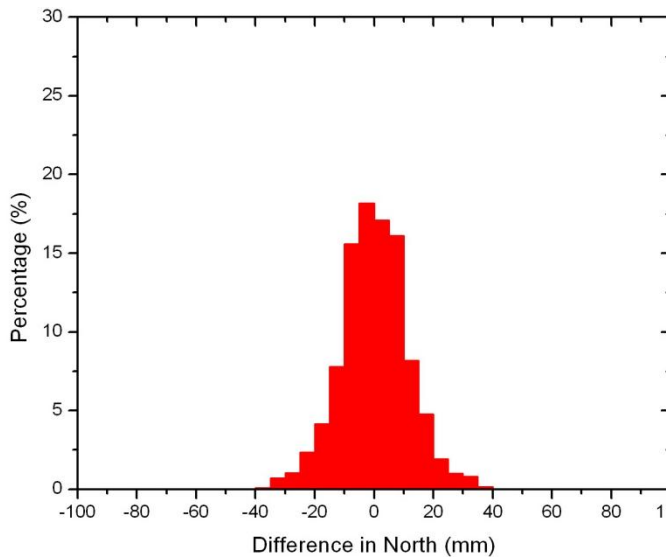
➤ Software

- iPPP in C++ for PPP + UPD + Regional Augmentation

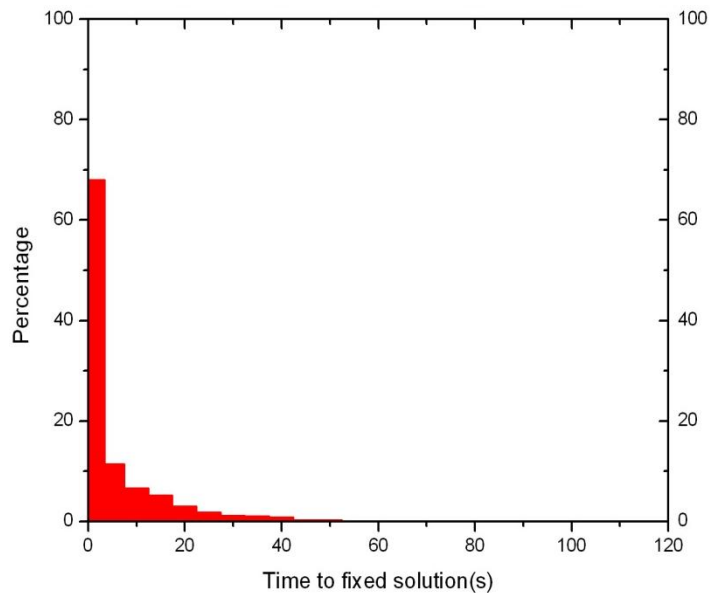
PPP With L1+L2+iono. Constraints



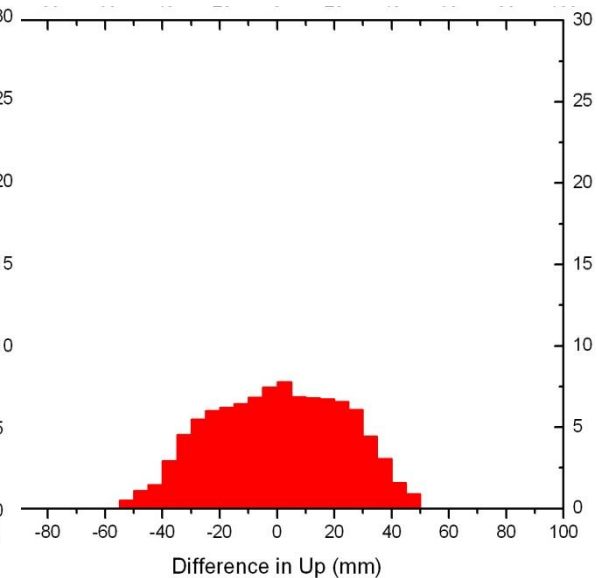
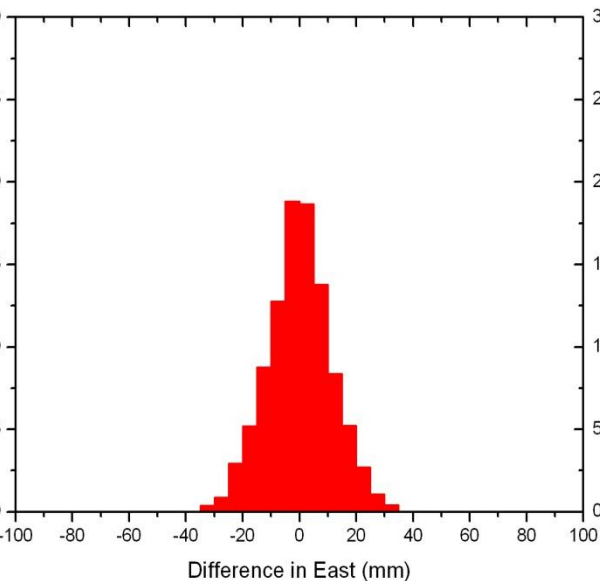
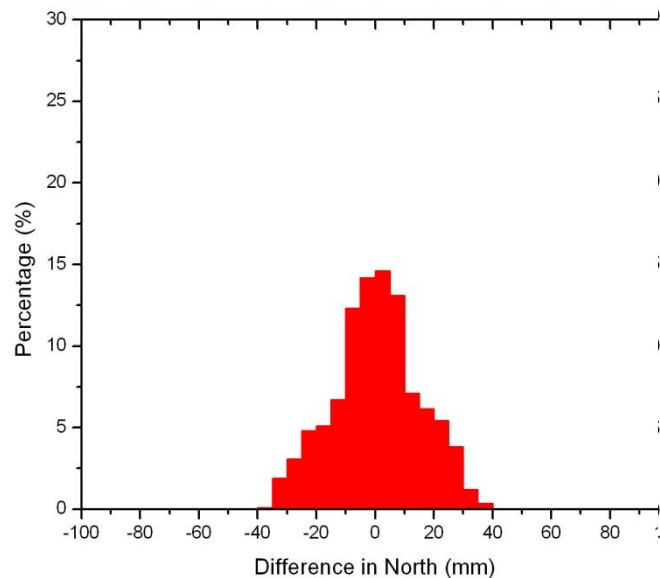
- Reset The Estimator Every Minute
- 87% Fixed With 1 Epoch, On Average Two Epochs
- 12, 10 and 25 mm in ENU



PPP With Lw+Lc Obs.

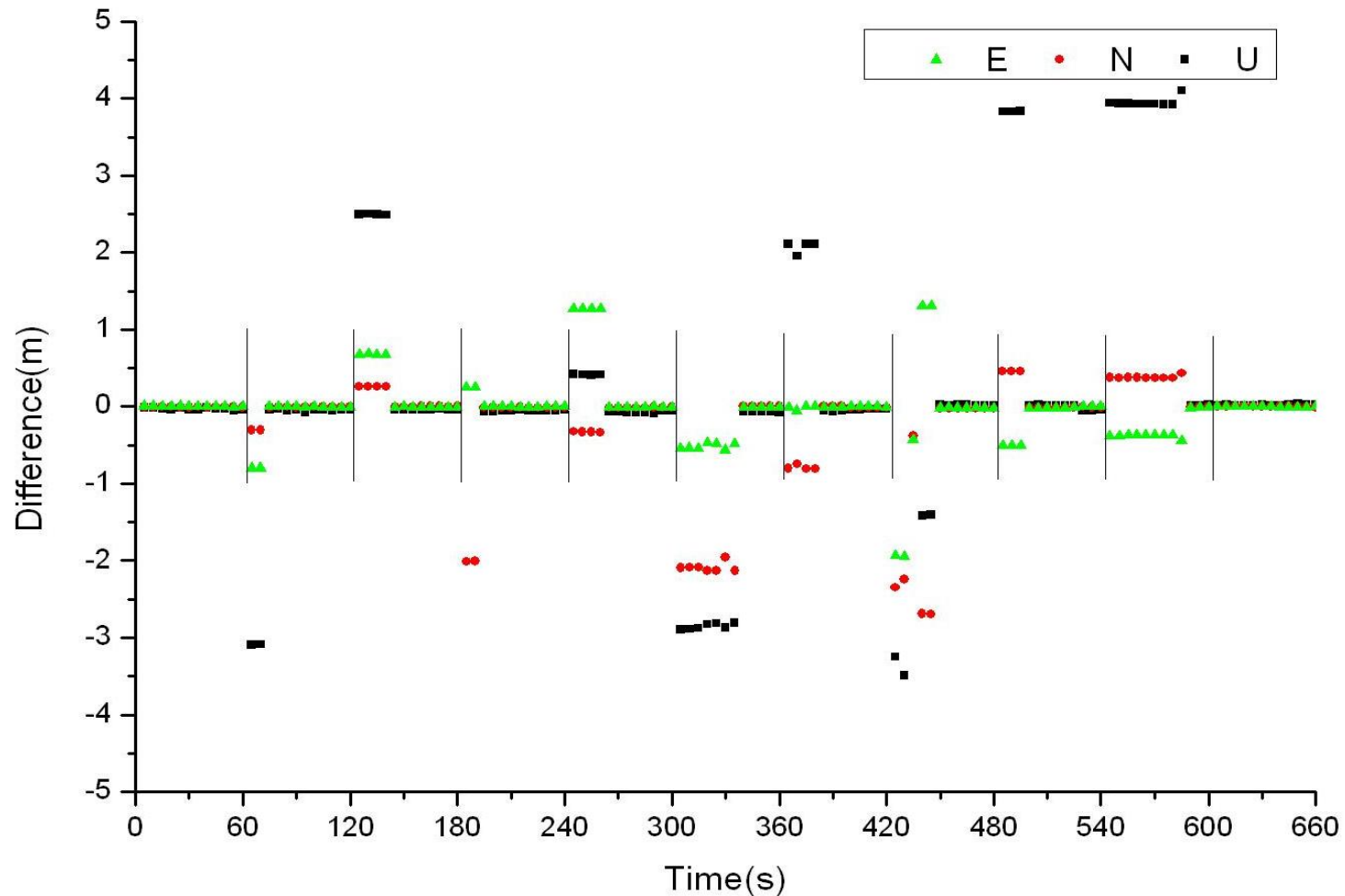


- Reset The Estimator Every Minute
- 68% Fixed With 1 Epoch, On Average Two Epochs
- 15, 10 and 30 mm in ENU

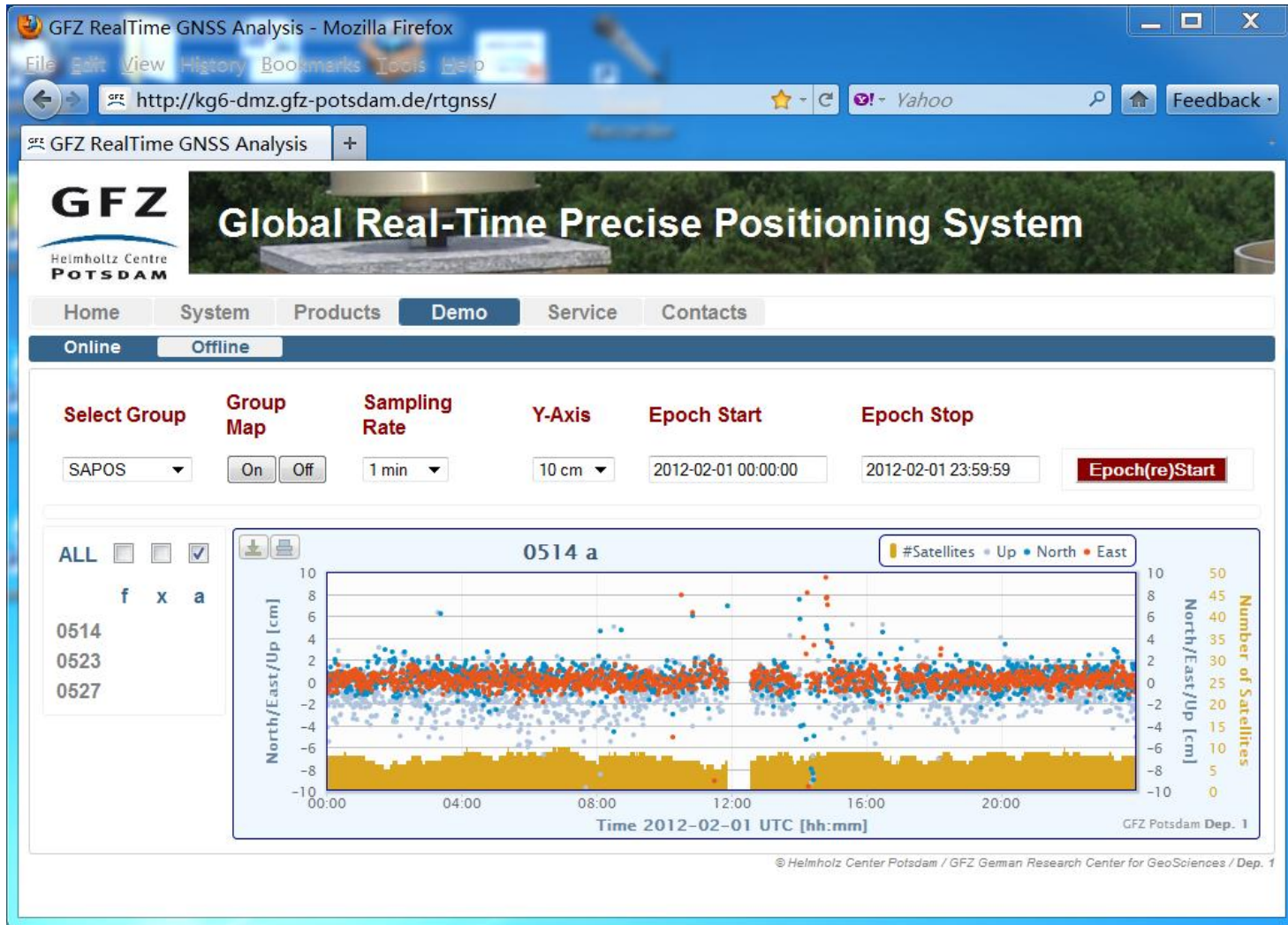


Example Of Real-Time Results

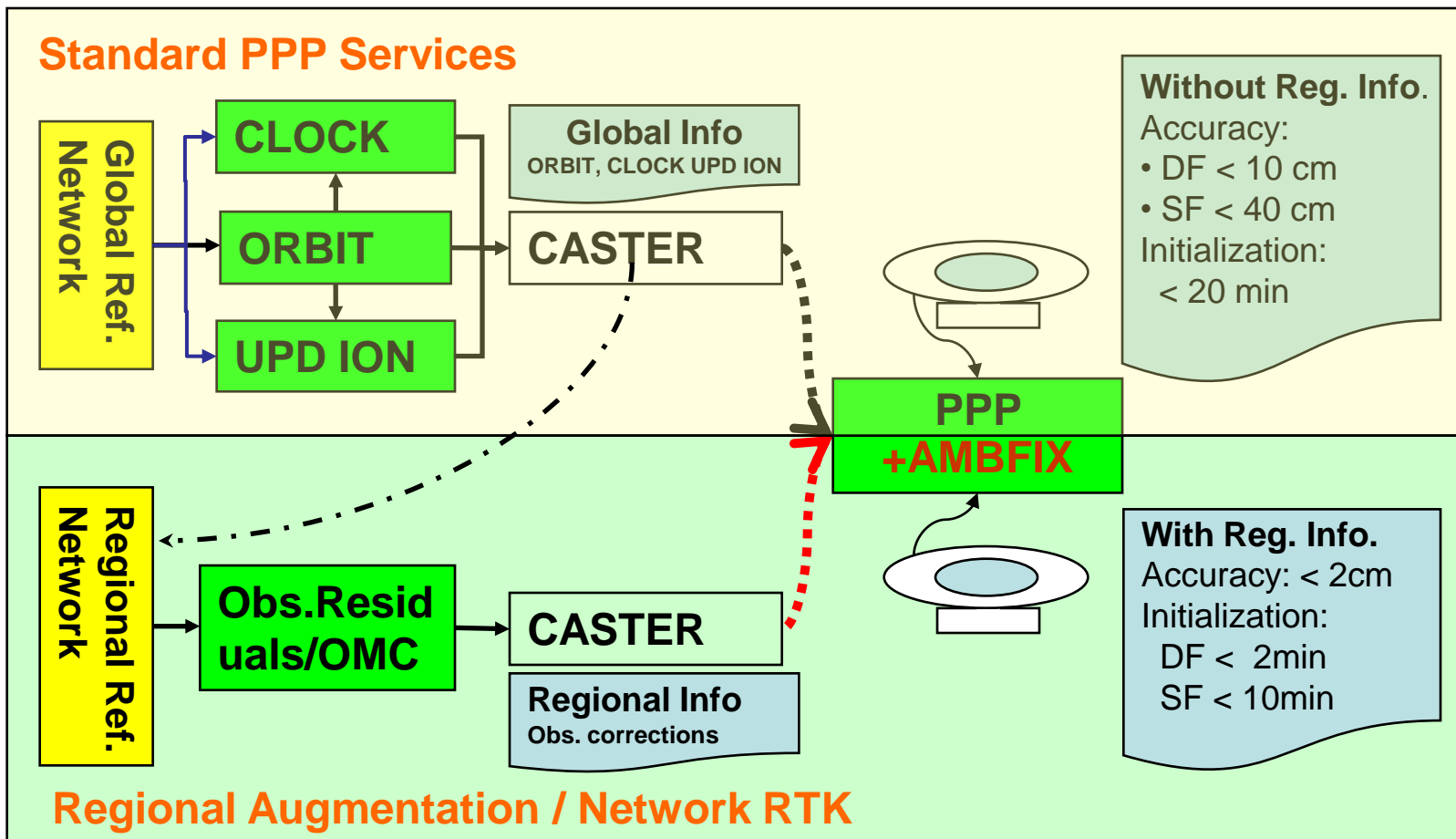
- Every Minute Reset The Estimator, Initial Coordinates from SPP



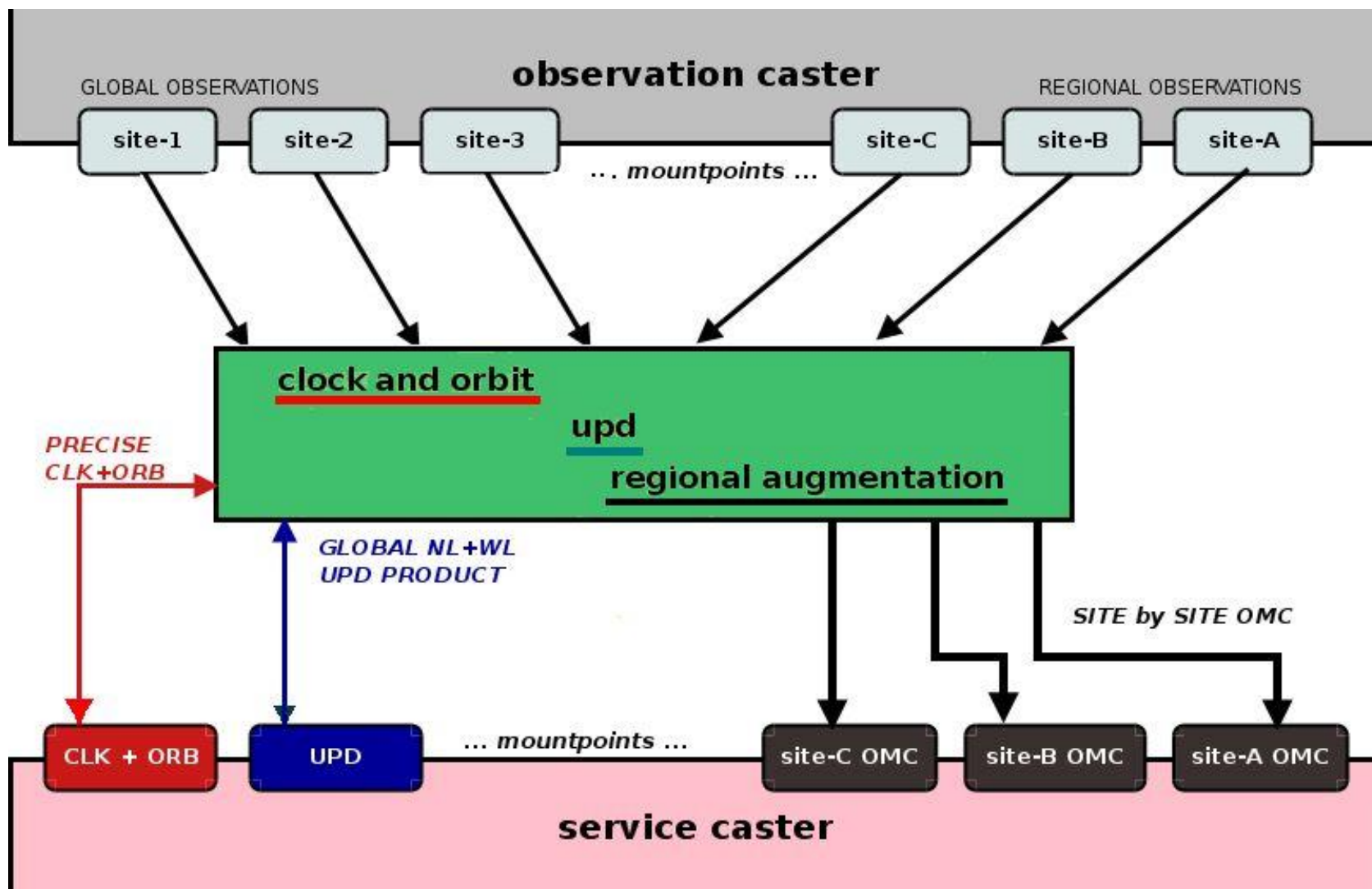
Example Of Real-Time Results



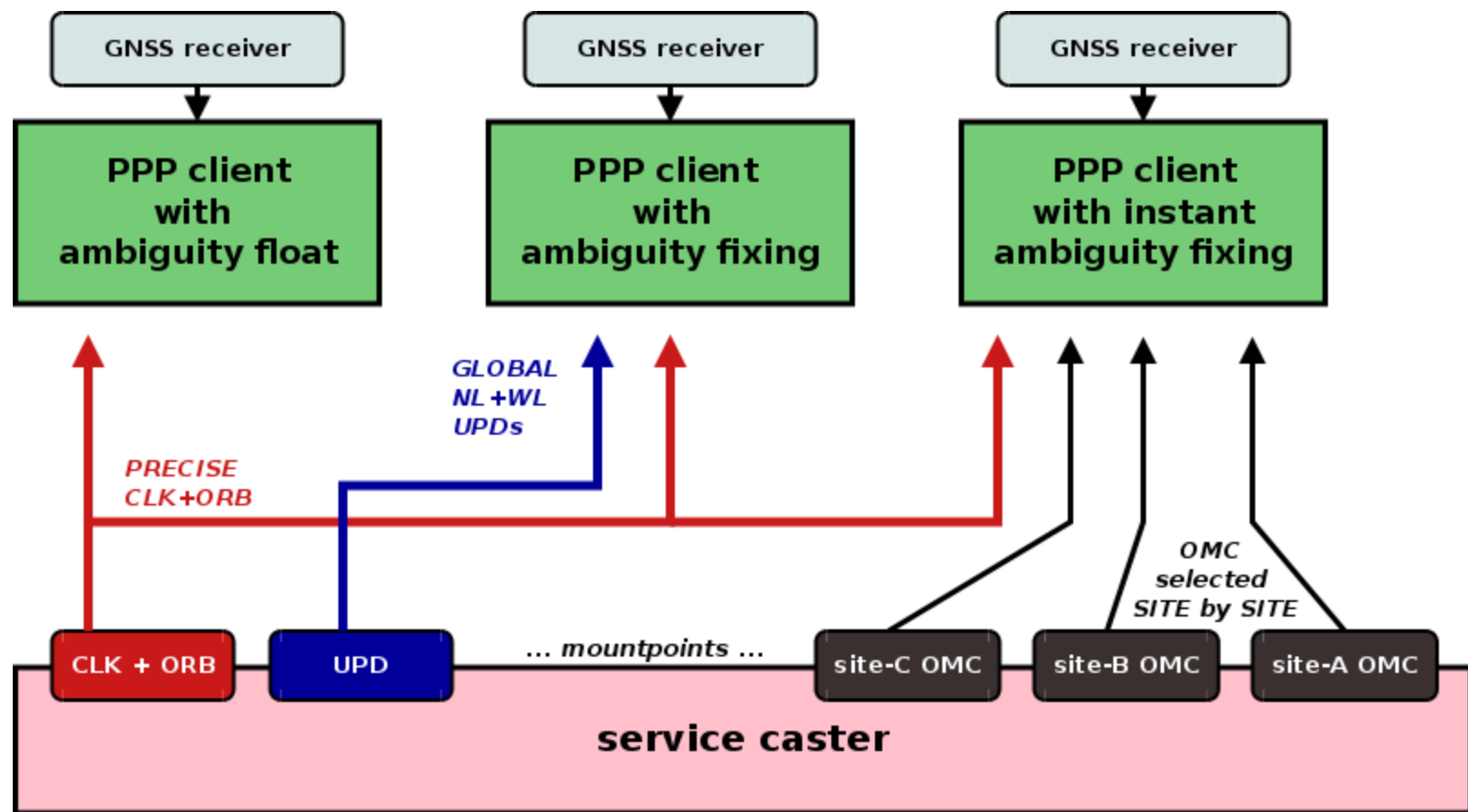
Augmentation of PPP Service



Global Real-Time Precise Point Positioning With Regional Augmentation



PPP Clients



Performance Of The Augmented PPP Service

- Without Regional Augmentation**
 - Open Ocean, ...
 - 5-10 cm, after 30 min., 3-5 cm after Ambiguity-Fixing (15 min)
- With Regional Augmentation**
 - Developed Cities, ...
 - 1-2 cm, within 1-2 min. depends on ...
- Also For Single-Frequency And Low-Cost Receivers**

Thanks

Thanks To SAPOS, BKG, IGS
For Providing Real-Time Data !

Thanks for Your Attention !

For Details And More Real-Time
Results (PPP, PPP+AR, PPP+RA)

<http://kg6-dmz.gfz-potsdam.de/rtgnss/>